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# Self-Consistent Power/Performance/Reliability Analysis for Copper Interconnects

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MARCO Interconnect Focus Center



# Interconnect Scaling

## • Scaling Trends

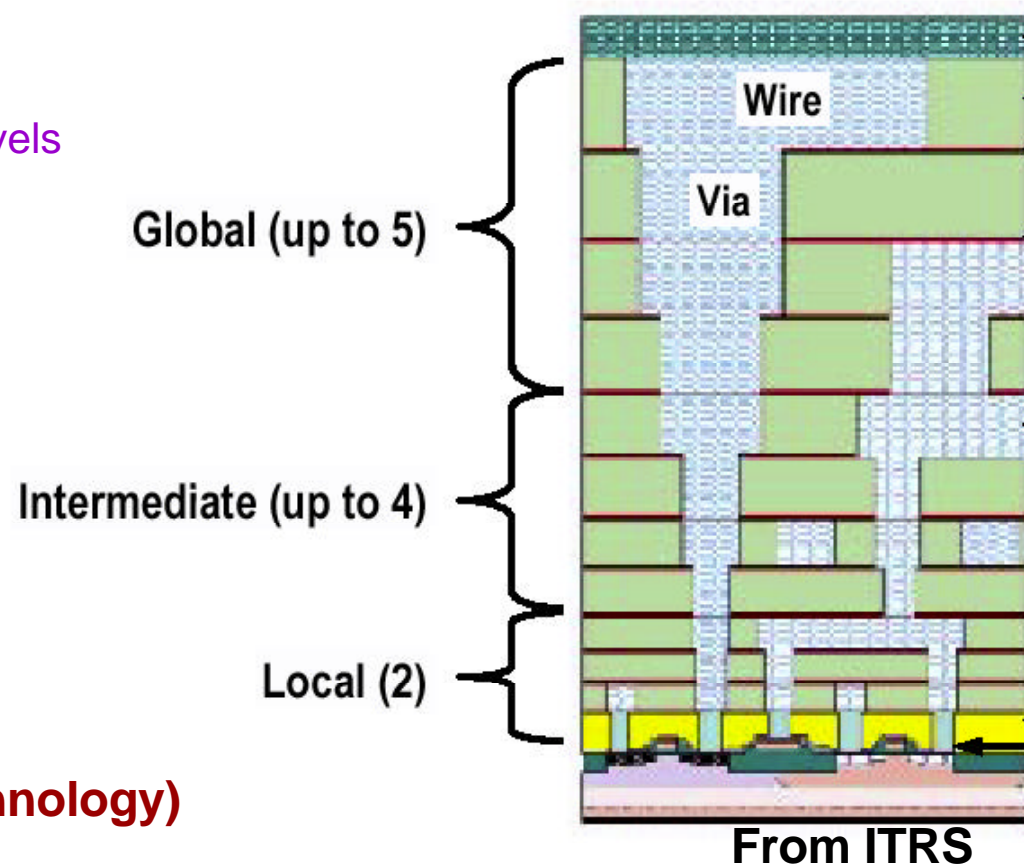
- More wires
- Shrinking and more metal levels
- Resistance & Capacitance  $\uparrow$   
⇒ Performance deteriorates

## • Metrics

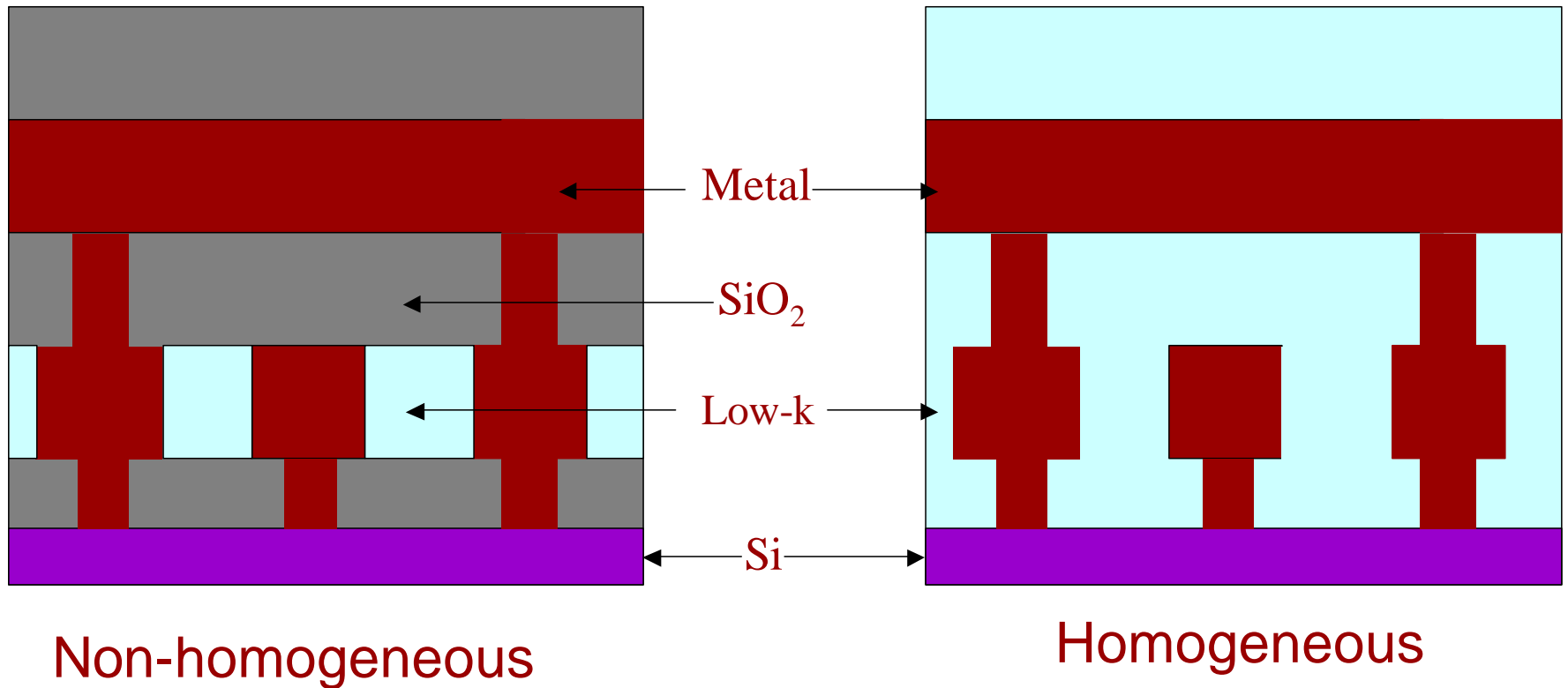
- Delay
- Power dissipation
- Cross talk (data reliability)
- Bandwidth
- Area
- Reliability

## • Mitigating Solutions (Technology)

- Al to Cu
- lower k: Two Methods



# Dielectric Technology



- Power: Homogeneous
- Cross talk: Non-homogeneous
- Delay:
  - local: C (homogeneous)
  - long distance: RC (Unclear?)

# Self-Consistent Temperature Distribution

- Fourier's Law

$$J^2 \mathbf{r}[T] \propto k_{\text{eff}}[T] \frac{dT}{dx}$$

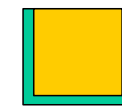
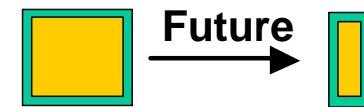
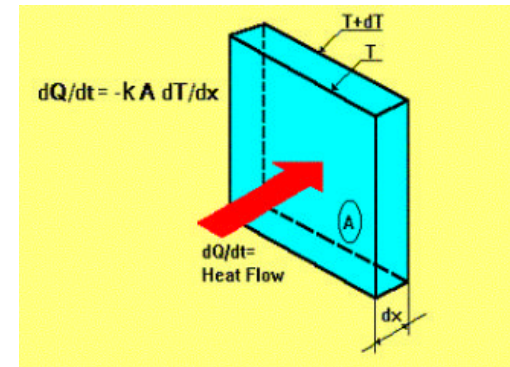
Ignored Before

- Electrical Resistance  $\propto \mathbf{r}[T]$

- Thermal Coefficient of Resistance
- Barrier, Surface Scattering
- Number of metal levels

- Thermal Resistance  $\propto 1/k_{\text{eff}}[T]$

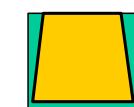
- Number of metal levels
- Via Effect



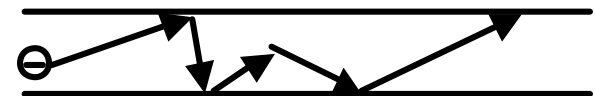
ALD



IPVD



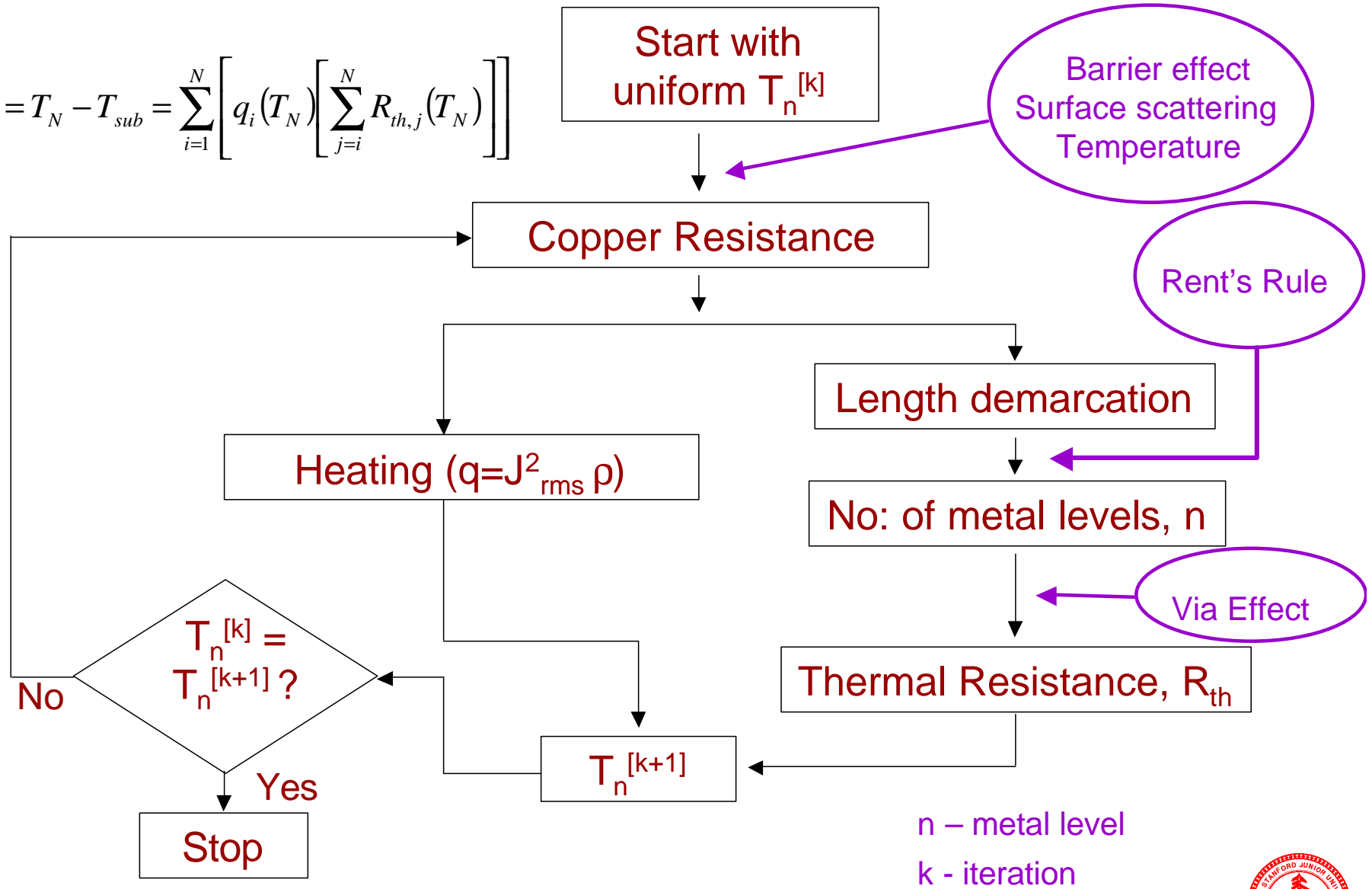
C-PVD



Given Current Density, J.

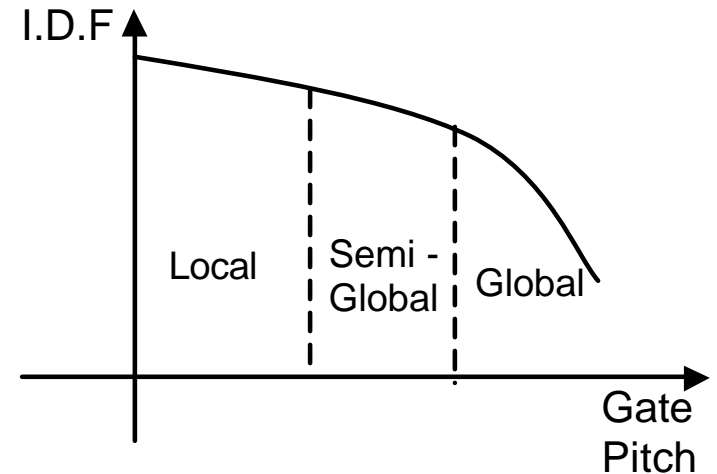
Find Temperature, T?

$$\Delta T_N = T_N - T_{sub} = \sum_{i=1}^N \left[ q_i(T_N) \left[ \sum_{j=i}^N R_{th,j}(T_N) \right] \right]$$

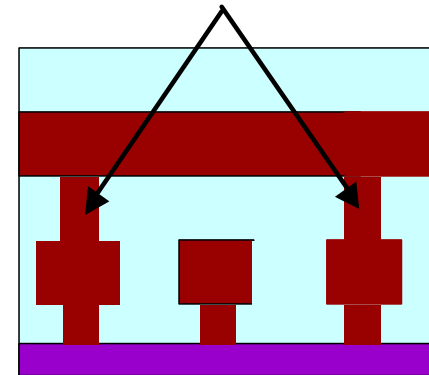


# Electrical & Thermal Resistance

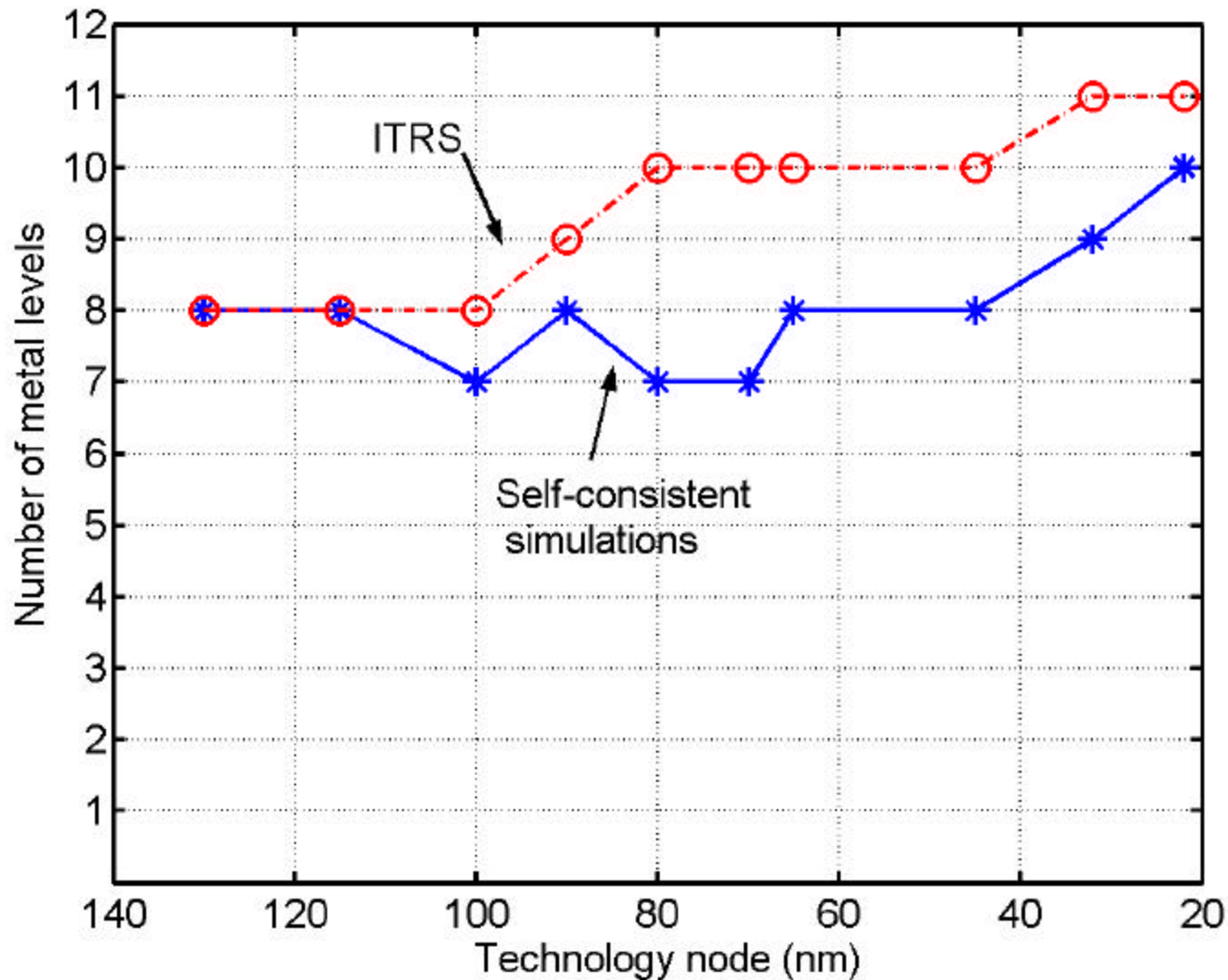
- Rent's Rule
  - Wire Length Distribution
- RC Wire Delay
  - Local, Semi-global, Global Demarcation
  - Number of metal levels
  - Stack Height
- Thermal Resistance
  - Stack Height
  - Via Effect



Efficient heat conductors  
(reduce thermal resistance)



# Number of Metal Levels

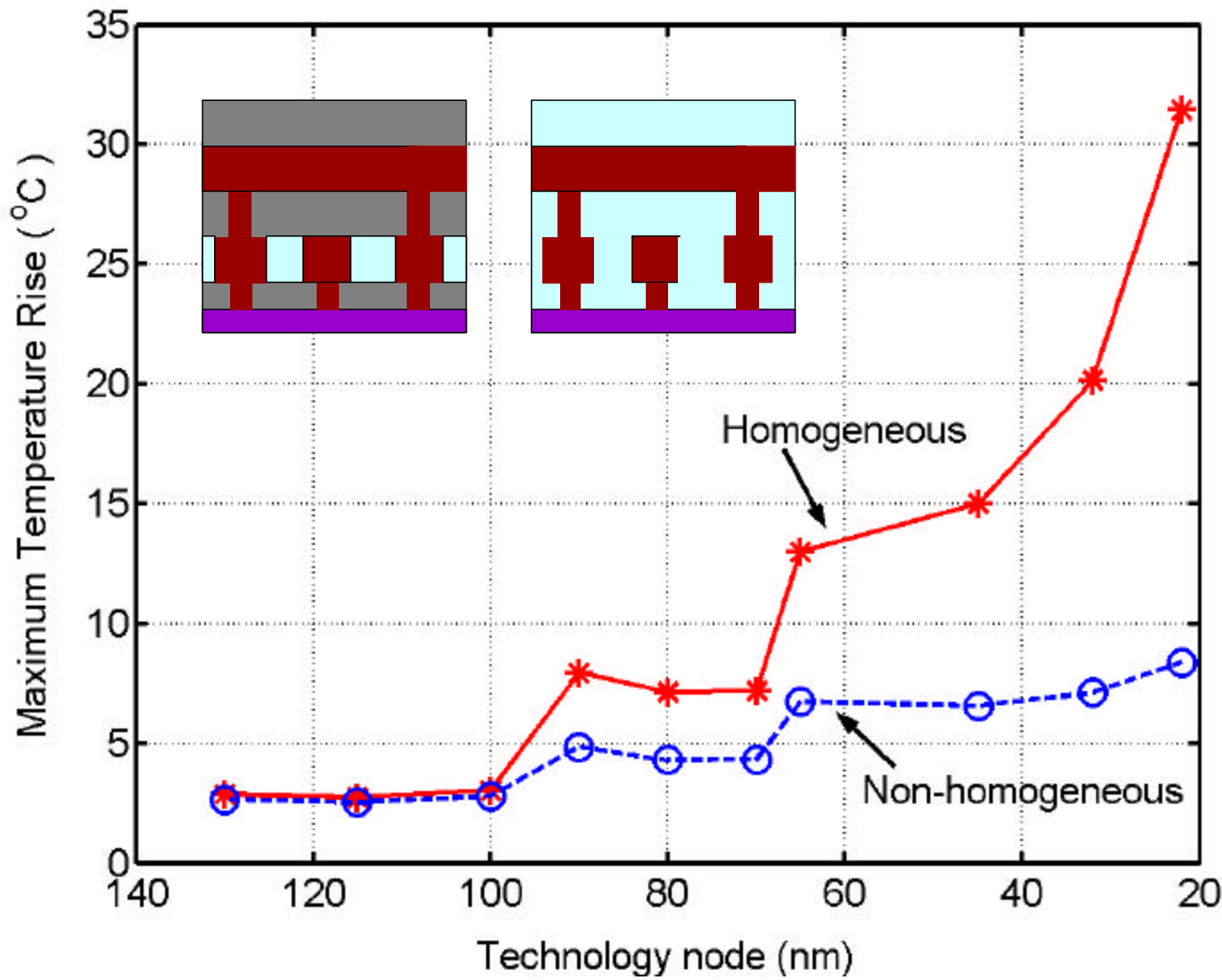


Fluctuations are artifacts of numerical calculations

Power, Ground & Clock lines not included



# Maximum Temperature Rise $\Delta T \propto J^2 \rho \times R_{Th}$



$\Delta T \sim 10 \times \uparrow$

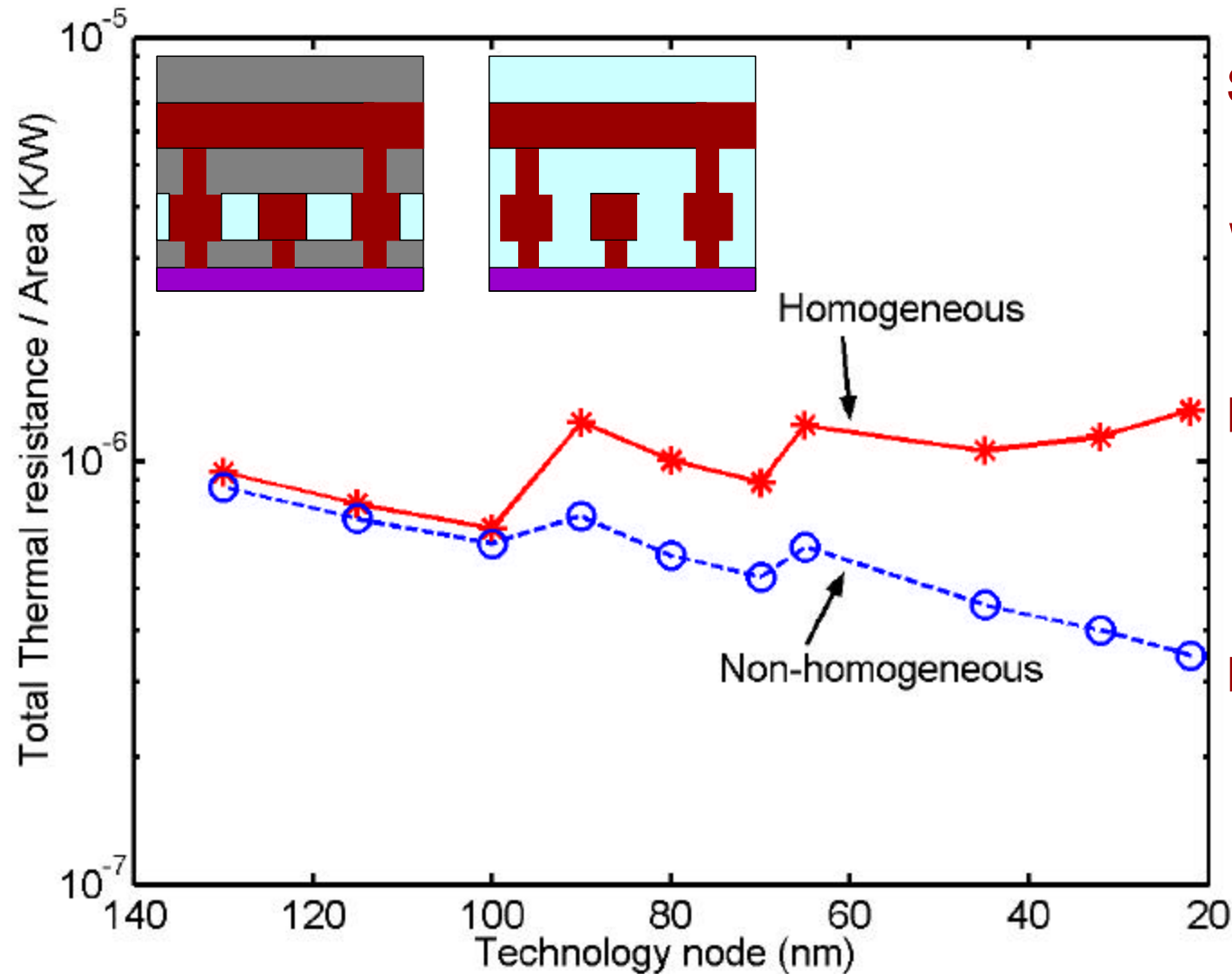
$\Delta T \sim 3 \times \uparrow$





# Effective Thermal Resistance

$$R_{th,eff} = \sum H_i / K_{eff, i}$$



Surprising decrease!

Wire thickness

$H \sim 4\times \downarrow$

$R_{th,eff} \sim 1.5\times \uparrow$

$K_{eff} \sim 3.5\times \downarrow$

Poor Conductivity of Low-k

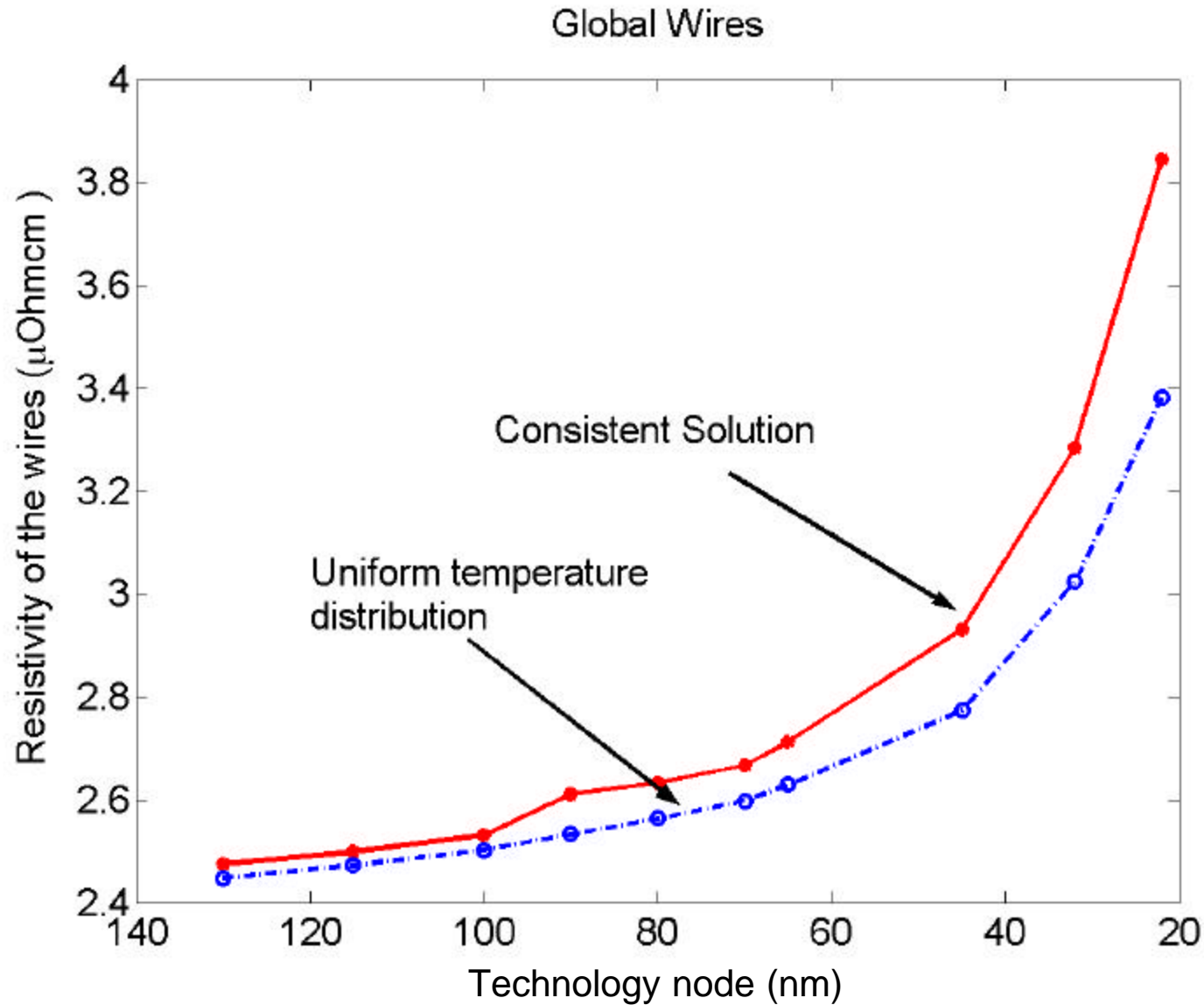
$R_{th,eff} \sim 3\times \downarrow$

$K_{eff} \sim \text{constant}$

High Conductivity of  $\text{SiO}_2$



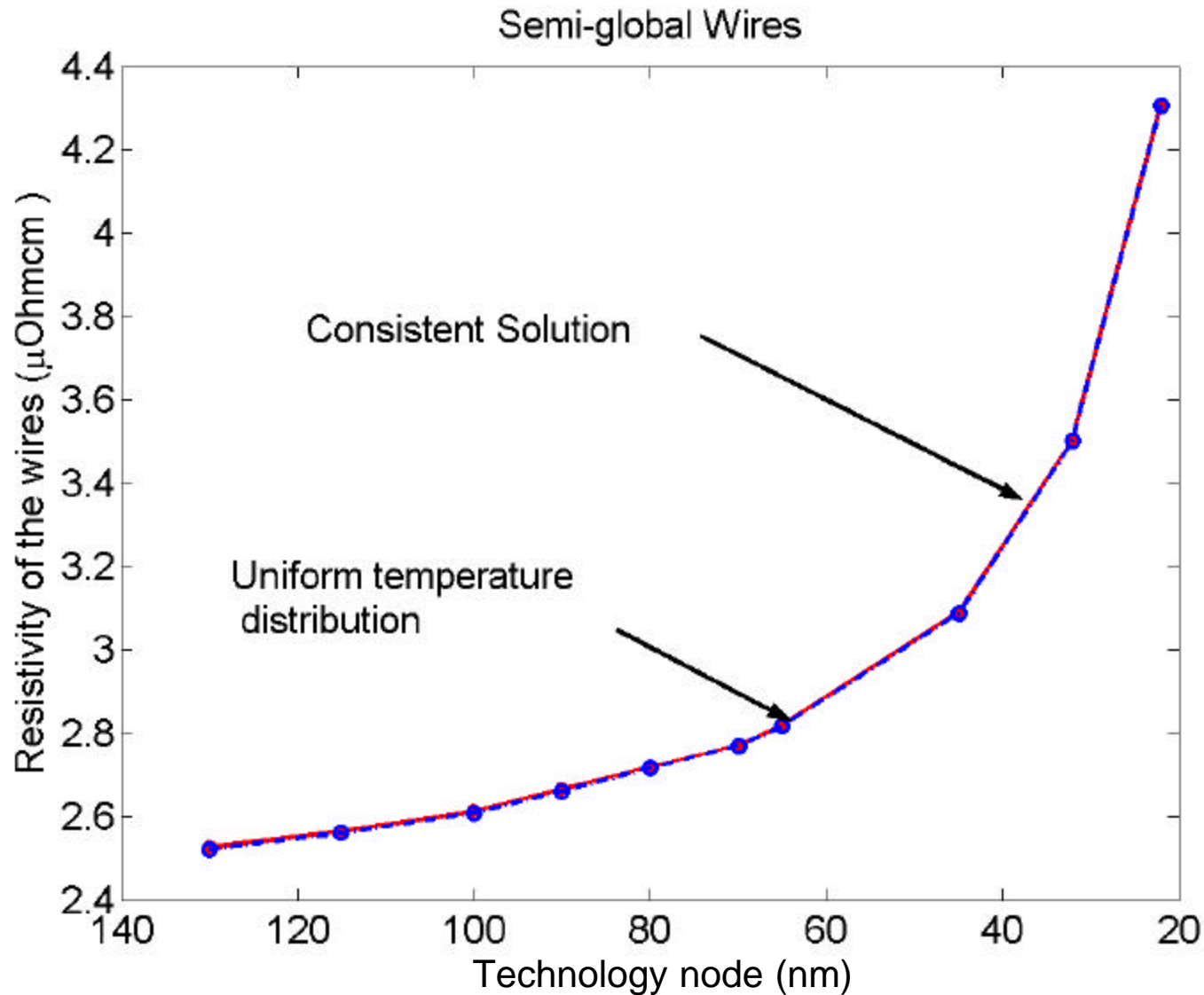
# Electrical Resistivity-Global Wires



Consistent Solution  
is larger by up to 15%



# Electrical Resistivity-Semi-Global Wires



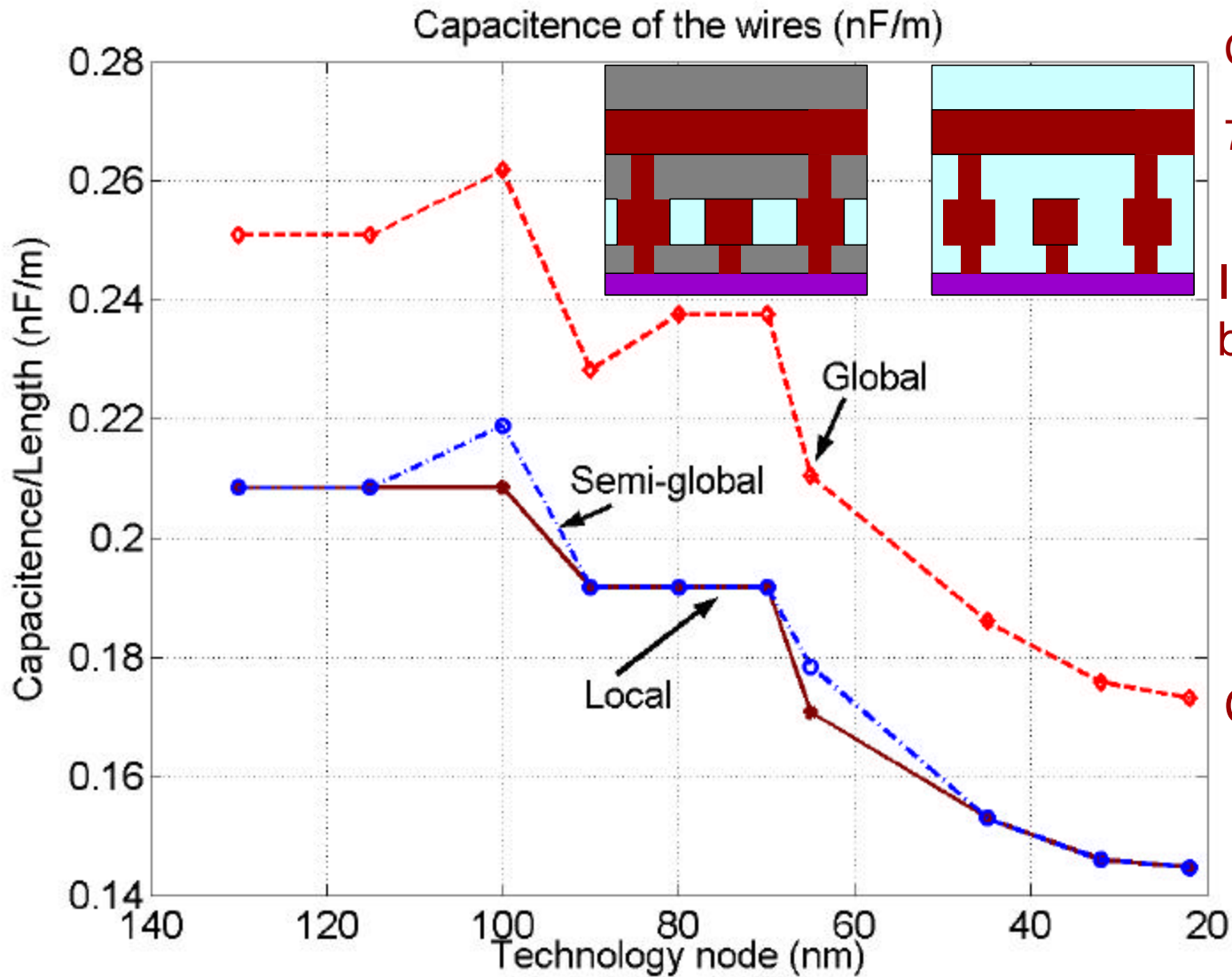
Negligible difference

Wire Temperature ~  
Substrate T

Smaller wire pitch  
⇒ Larger via density



# Wire Capacitance



$$C_{\text{total}} = C_{\text{IMD}} + C_{\text{ILD}}$$

$$70\% \text{ of } C_{\text{total}} = C_{\text{IMD}}$$

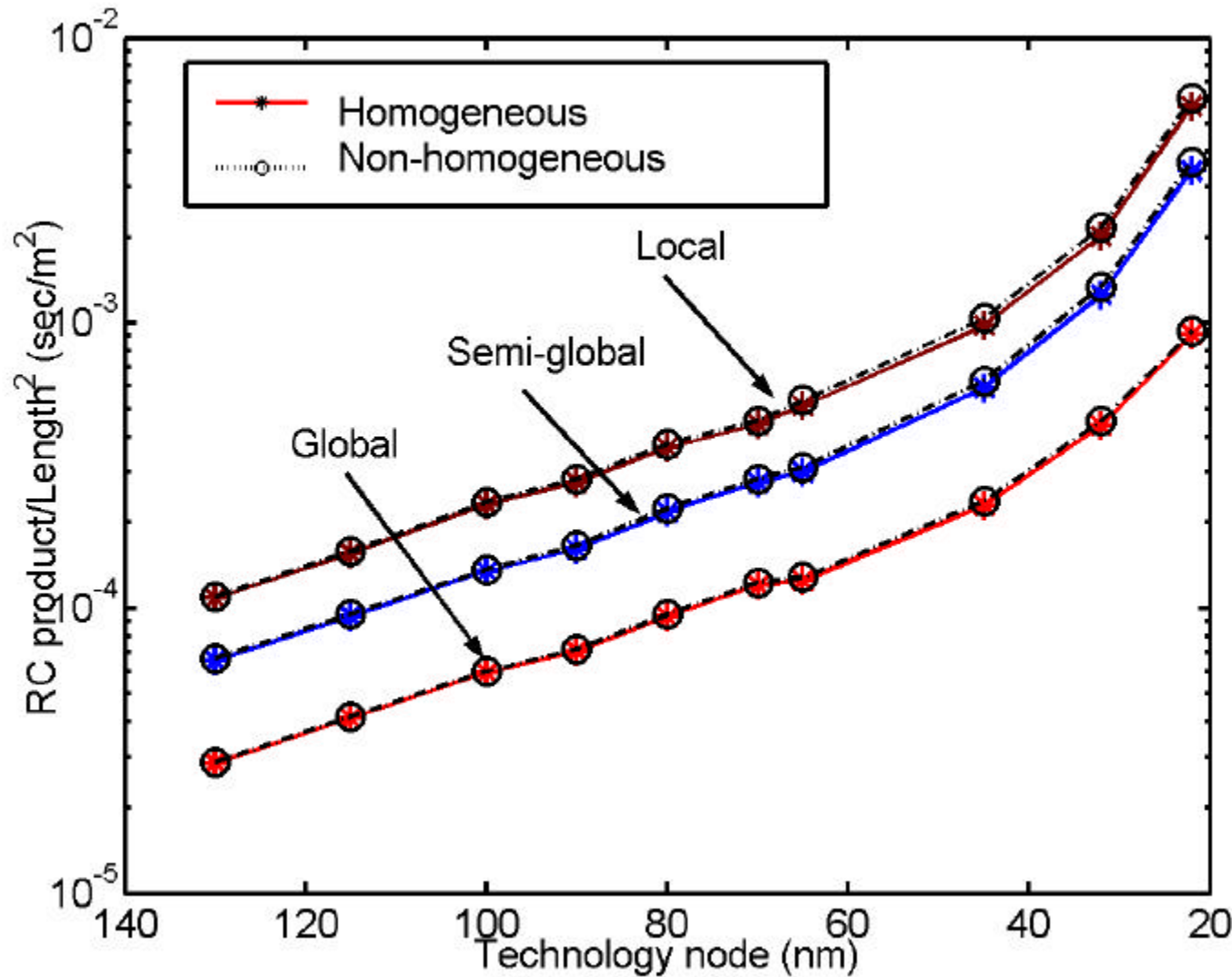
IMD is Low-k for both cases

Capacitance  $1.6\times \downarrow$

$$\epsilon_{\text{IMD}} \sim 2\times \downarrow$$



# Delay Metric - $RC/L^2$



$R/\text{Length} \sim 50\times \uparrow$   
 $C/\text{Length} \sim 1.6\times \downarrow$

Capacitance advantage of homogeneous is offset by the increased resistance

Is that all?  
Reliability

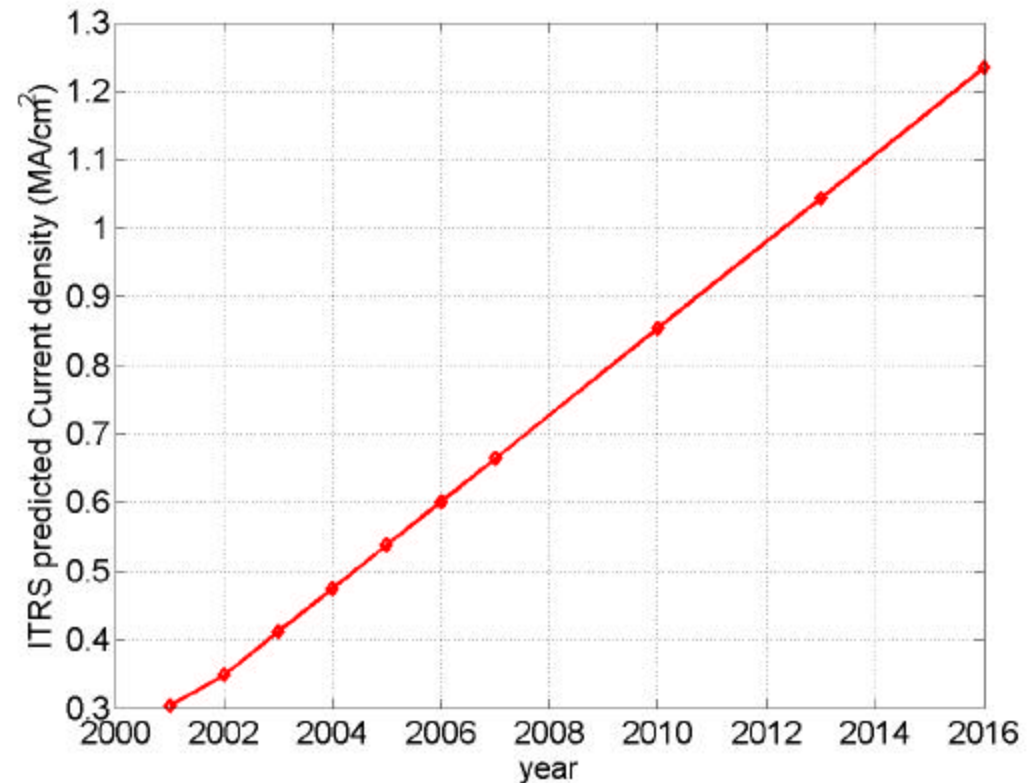


# Can Current Density go on Increasing?

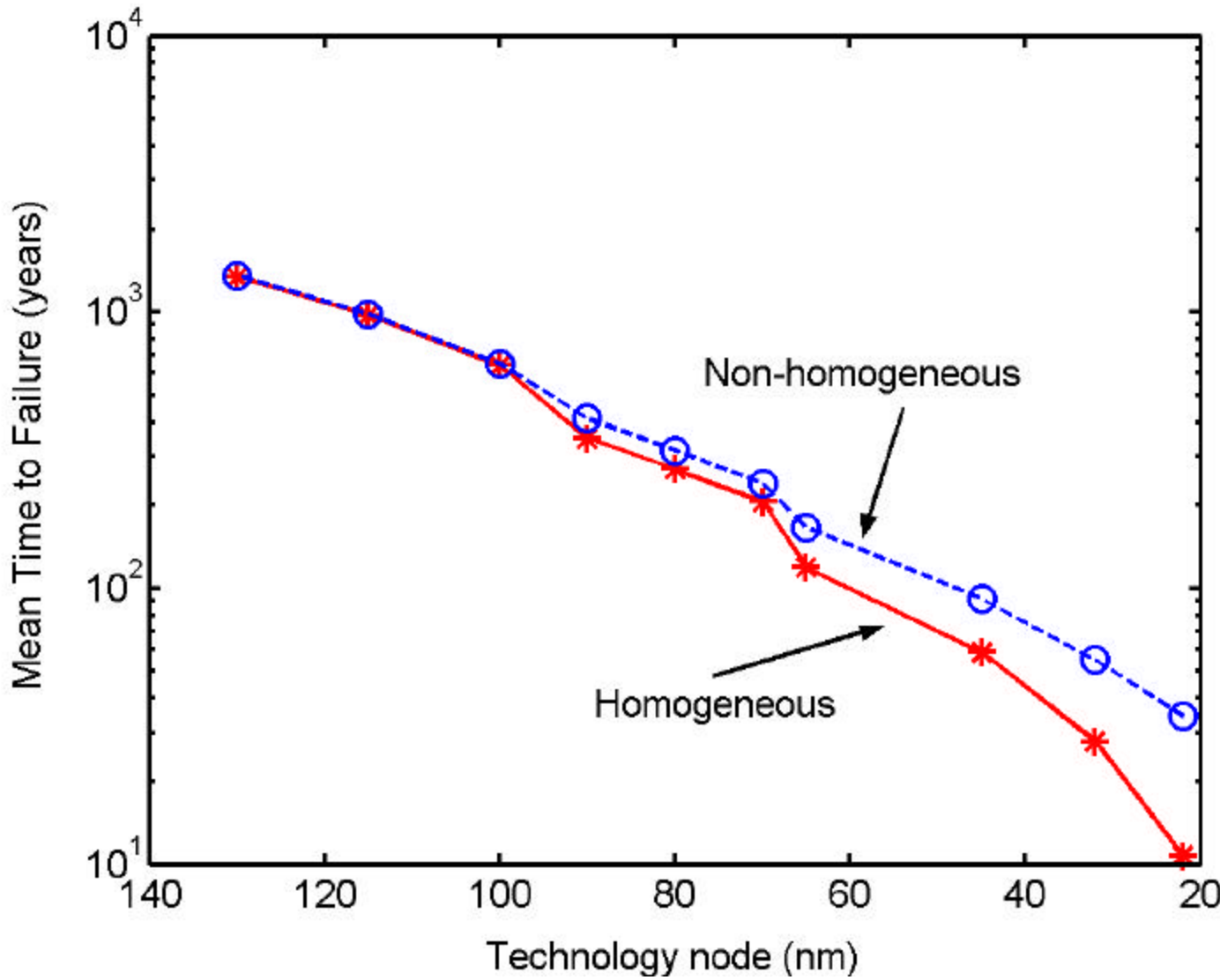
- Required Current
  - Integration density
- Allowed Current
  - Electromigration
  - IR drop in supply voltage

- Black's Law
$$MTF = AJ_{avg}^{-n} \exp\left(\frac{E_a}{kT}\right)$$

If  $J \uparrow \Rightarrow T \uparrow$   
 $\Rightarrow MTF \downarrow$



# Mean Time to Failure



Larger Temperature  
 ⇒ Lower MTF

Non-homogeneous  
 is better.

Reliability  
 Cross-talk

$$X_{talk} \propto \frac{1}{1 + \frac{e_{ILD} / e_{IMD}}{A.R^2}}$$



# Is there a consistent solution?

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- Black's Law

$$MTF = AJ_{avg}^{-n} \exp\left(\frac{E_a}{kT}\right)$$

- Joule Heating

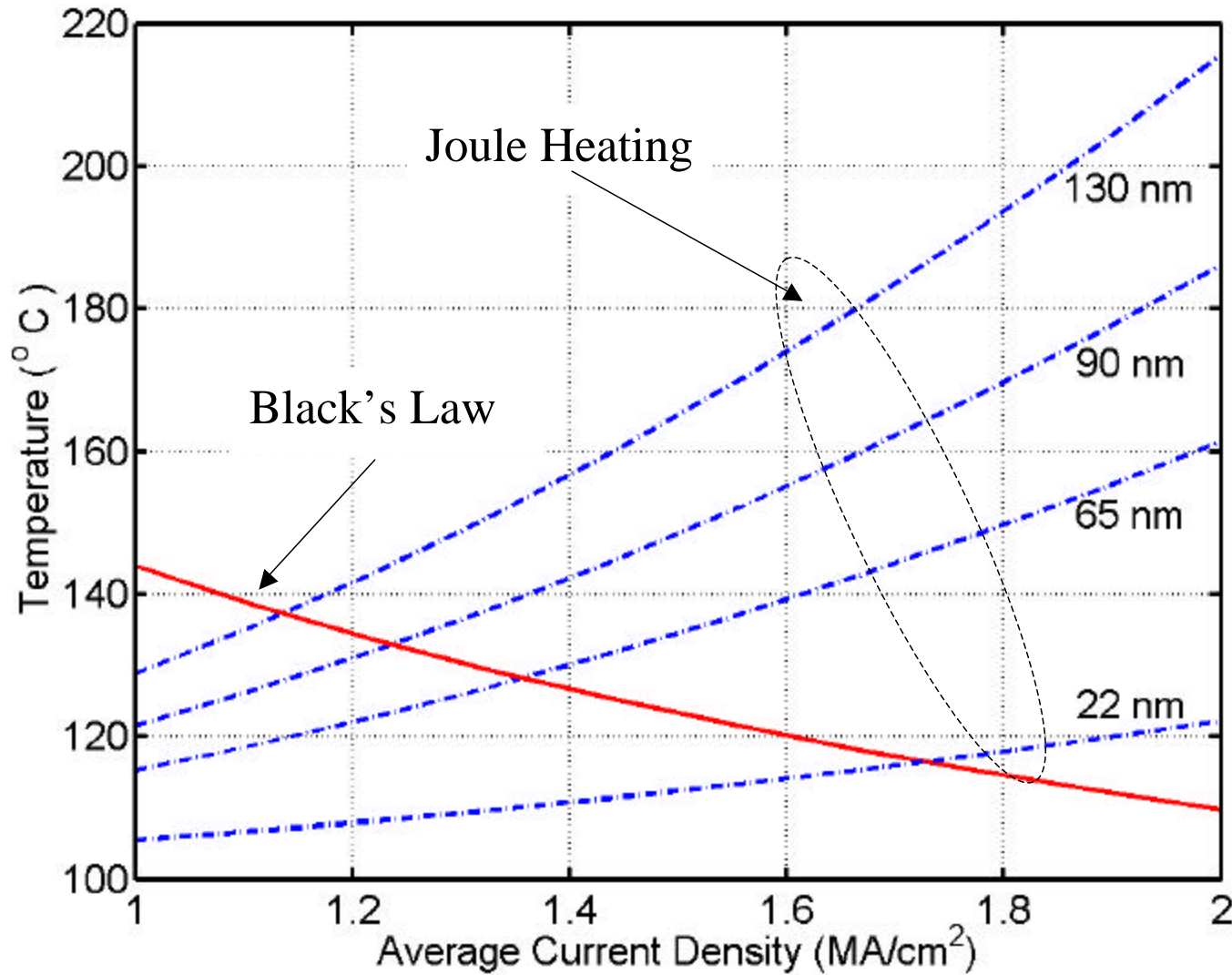
$$J_{rms}^2 \mathbf{r}[T] \propto k_{eff}[T] \frac{dT}{dx}$$

$$J_{avg}^2 = r J_{rms}^2 \quad r - \text{Duty Cycle}$$





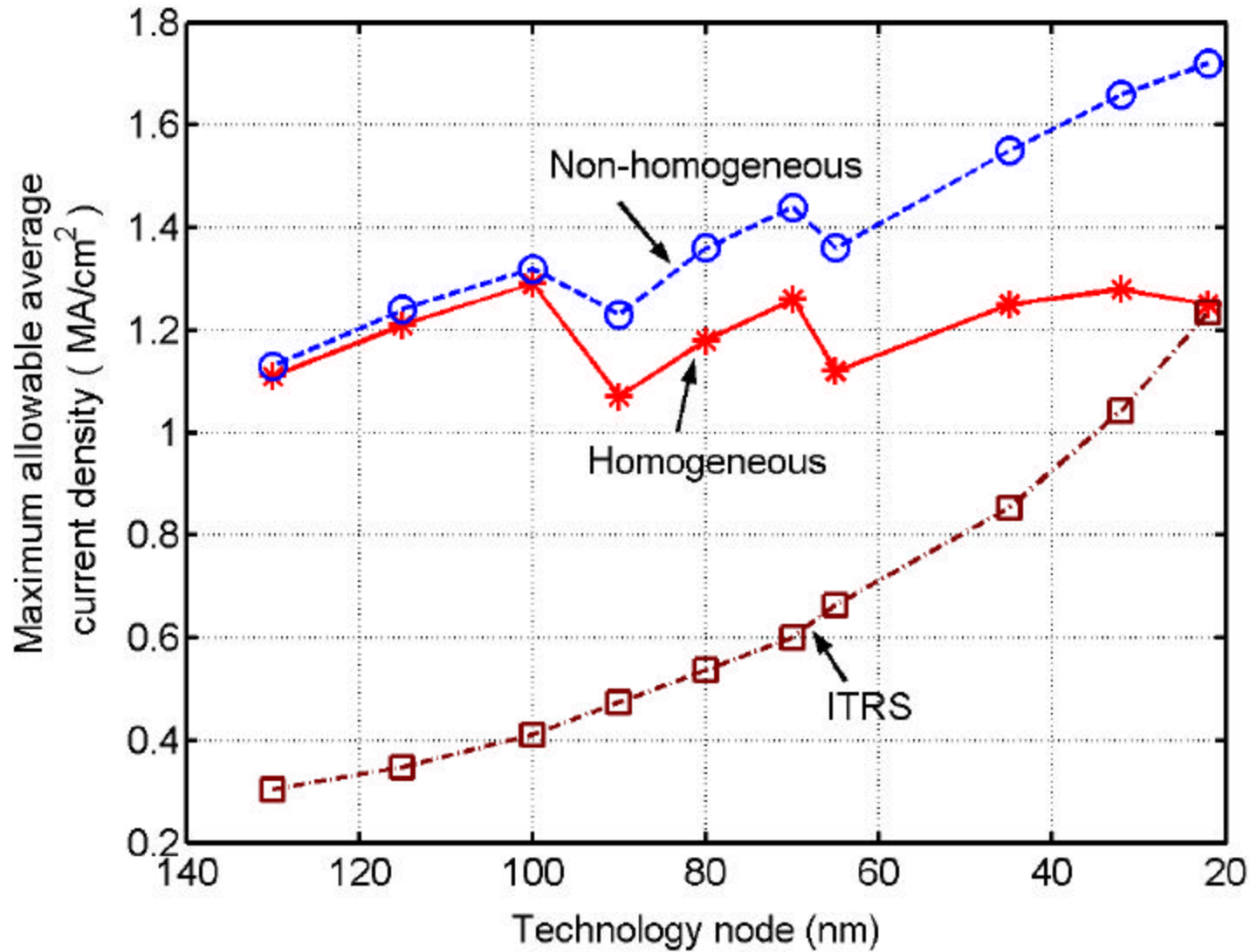
# Consistent Solution



Point of intersection is the consistent solution



# Consistent Solution



# Conclusion

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- Consistent Algorithm to estimate
  - Thermal Profiles
  - Electromigration constraints
- Comparison of Dielectric Technologies
  - Power, Delay - Homogeneous
  - Cross-talk, Reliability – Non-homogeneous



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Thank You

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14 February, 2004

SLIP, 2004

